

## pH Calculations during neutralisation and dilution

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### Working out pH by part neutralising a strong acid with a strong base

We start with a strong acid. Some of it is neutralised.

What are we left with?

A strong acid but fewer moles, so lower concentration

The pH will be higher

50cm<sup>3</sup> of 1M HCl is reacted with 30cm<sup>3</sup> of 0.7M NaOH.  
What will be the pH of the resulting mixture?

## Working out pH by part neutralising a strong acid with a strong base

First we need to work out how many moles of acid is left.

- work out number of moles in original acid  
moles = conc x vol =  $1 \times 50/1000 = 0.05\text{mol}$
- work out number of moles in base added  
moles = conc x vol =  $0.7 \times 30/1000 = 0.021\text{mol}$
- work out moles of acid left by subtracting base moles from acid moles ( will need to convert moles if not 1:1 ratio)  
Moles HCl left =  $0.05 - 0.021 = 0.029\text{ mol}$

- work out new concentration of remaining acid by dividing the remaining moles by new total volume (vol acid + vol alkali added)

$$\text{Conc HCl} = 0.029 / (80/1000) = 0.3625\text{M}$$

- work out conc of  $\text{H}^+$  and put in pH equation

As strong acid with complete dissociation

$$\text{Conc H}^+ = 0.3625\text{M}$$

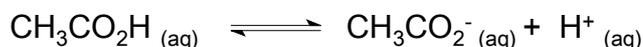
$$\begin{aligned}\text{pH} &= -\log [\text{H}^+] \\ &= -\log [0.3625] \\ &= 0.44\end{aligned}$$

## Working out pH by part neutralising a weak acid with a strong base

We start with a weak acid. Some of it is neutralised.

What are we left with?

A weak acid but fewer moles, so lower concentration, but because weak acids are equilibria we must use the  $K_a$  expression and also consider what effect the salt formed  $A^-$  has on the equilibrium amount of  $H^+$  ions



50cm<sup>3</sup> of 1M CH<sub>3</sub>COOH is reacted with 30cm<sup>3</sup> of 0.7M NaOH. What will be the pH of the resulting mixture?

## Working out pH by part neutralising a weak acid with a strong base

First we need to work out how many moles of acid is left.

This is exactly the same as in the strong acid case

- work out number of moles in original weak acid  
moles = conc x vol = 1 x 50/1000 = 0.05mol
- work out number of moles in base added  
moles = conc x vol = 0.7 x 30/1000 = 0.021mol
- work out moles of acid left by subtracting base moles from acid moles ( will need to convert moles if not 1:1 ratio)

Moles CH<sub>3</sub>COOH left = 0.05-0.021 = 0.029 mol

- work out new concentration of remaining acid by dividing the remaining moles by new total volume (vol acid + vol alkali added)

$$\text{Conc CH}_3\text{COOH} = 0.029 / (80/1000) = 0.3625\text{M}$$

- work out moles of salt formed from the balanced equation

1 mole of OH<sup>-</sup> give 1 mole of salt formed

0.021 moles OH<sup>-</sup> gives 0.021 moles of CH<sub>3</sub>COO<sup>-</sup>

- work out concentration of salt formed by dividing the moles of salt by new total volume (vol acid + vol alkali added)

$$\text{Conc CH}_3\text{COO}^- = 0.021 / (80/1000) = 0.2625\text{M}$$

Put values of K<sub>a</sub>, and concs of acid and salt into equilibrium expression to work out conc of H<sup>+</sup>

$$K_a = \frac{[\text{H}^+_{(aq)}][\text{CH}_3\text{CO}_2^-_{(aq)}]}{[\text{CH}_3\text{CO}_2\text{H}_{(aq)}]} \quad [\text{H}^+_{(aq)}] = K_a \frac{[\text{HA}_{(aq)}]}{[\text{A}^-_{(aq)}]}$$

$$[\text{H}^+_{(aq)}] = 1.7 \times 10^{-5} \frac{0.3625}{0.2625} = 2.348 \times 10^{-5}$$

put in pH equation

$$\begin{aligned} \text{pH} &= -\log [\text{H}^+] \\ &= -\log [2.348 \times 10^{-5}] \\ &= 4.63 \end{aligned}$$

### Working out pH of a weak acid at half equivalence

When a weak acid has been reacted with exactly half the neutralisation volume of alkali, the calculation can be simplified considerably.

$$[\text{H}^+_{(\text{aq})}] = K_a \frac{[\text{HA}_{(\text{aq})}]}{[\text{A}^-_{(\text{aq})}]}$$

At half neutralisation we can make the assumption that  $[\text{HA}] = [\text{A}^-]$

So  $[\text{H}^+_{(\text{aq})}] = K_a$  And  $\text{pH} = \text{p}K_a$

What is the pH of the resulting solution when  $25\text{cm}^3$  of  $0.1\text{M}$  NaOH is added to  $50\text{cm}^3$  of  $0.1\text{M}$   $\text{CH}_3\text{COOH}$  ( $K_a$   $1.7 \times 10^{-5}$ )

$$\text{pH} = -\log(1.7 \times 10^{-5}) = 4.77$$

### Working out pH by adding excess alkali when neutralising a strong or weak acid

We start with acid (strong or weak). We add more strong alkali than is needed to neutralise the acid .

What are we left with?

A strong alkali

$30\text{cm}^3$  of  $0.8\text{M}$  HCl is reacted with  $60\text{cm}^3$  of  $0.7\text{M}$  NaOH. What will be the pH of the resulting mixture?

## Working out pH by adding excess alkali when neutralising a strong or weak acid

First we need to work out how many moles of alkali is left.

- work out number of moles in original acid  
moles = conc x vol =  $0.8 \times 30/1000 = 0.024\text{mol}$
- work out number of moles in base added  
moles = conc x vol =  $0.7 \times 60/1000 = 0.042\text{mol}$
- work out moles of base left by subtracting acid moles from base moles ( will need to convert moles if not 1:1 ratio)  
Moles NaOH left =  $0.042 - 0.024 = 0.018\text{ mol}$

- work out new concentration of remaining alkali by dividing the remaining moles by new total volume (vol acid + vol alkali added)

$$\text{Conc NaOH} = 0.018 / (90/1000) = 0.2\text{M}$$

- use Kw expression to work out  $[\text{H}^+]$

$$K_w = [\text{H}^+_{(\text{aq})}][\text{OH}^-_{(\text{aq})}] = 1 \times 10^{-14}$$

$$[\text{H}^+_{(\text{aq})}] = k_w / [\text{OH}^-_{(\text{aq})}] = 1 \times 10^{-14} / 0.2 = 5 \times 10^{-14} \text{ M}$$

put in pH equation

$$\begin{aligned} \text{pH} &= -\log [\text{H}^+] \\ &= -\log [5 \times 10^{-14}] \\ &= 13.3 \end{aligned}$$

## Diluting an acid or alkali

1. work out number of moles in original acid (conc x vol)
2. work out new concentration by dividing the moles by new total volume (initial volume + what volume water that has been added)
3. calculate pH of new concentration of acid using appropriate method i.e strong acid/weak acid/ strong base

Or more simply

### **pH of diluted strong acid**

$$[\text{H}^+] = [\text{H}^+]_{\text{old}} \times \frac{\text{old volume}}{\text{new volume}}$$

$$\text{pH} = -\log [\text{H}^+]$$

### **pH of diluted base**

$$[\text{OH}^-] = [\text{OH}^-]_{\text{old}} \times \frac{\text{old volume}}{\text{new volume}}$$

$$[\text{H}^+] = \frac{K_w}{[\text{OH}^-]}$$

$$\text{pH} = -\log [\text{H}^+]$$